

Injection of a cold atomic beam into a magnetic guide

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We report the continuous or pulsed loading of a slow and cold atomic beam into a magnetic guide. In order to optimize the transfer into the guide, we have studied two coupling schemes. The first one is based on an auxiliary two-dimensional MOT that confines the atoms transversally before they enter the guide. However, for low atomic velocities, the atoms are strongly heated in the longitudinal direction. This limitation does not occur in the second coupling scheme which relies on magnetic confinement in the transfer zone. For this purpose, we have constructed a miniature magnetic guide located between the atomic source and the long magnetic guide. The latter scheme allows to inject atoms with velocities down to 70 cm/s into the guide.

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A spectacular challenge in the field of Bose-Einstein condensation consists in the achievement of a continuous beam operating in the quantum degenerate regime. This would be the matter wave equivalent of a cw monochromatic laser and it would allow for unprecedented performances in terms of focalization or collimation. In [1], a continuous source of Bose-Einstein condensed atoms was obtained by periodically replenishing a condensate held in an optical dipole trap with new condensates. This kind of technique raises the possibility of realizing a continuous atom laser. An alternative way to achieve this goal has been studied theoretically in [2]. A non-degenerate, but already slow and cold beam of particles, is injected into a magnetic guide [3, 4, 5, 6, 7, 8, 9, 10] where transverse evaporation takes place. If the elastic collision rate is large enough, efficient evaporative cooling can lead to quantum degeneracy at the exit of the guide. The condition for reaching degeneracy with this scheme can be formulated by means of three parameters: the length ℓ of the magnetic guide on which evaporative cooling is performed, the collision rate γ at the beginning of the evaporation stage, and the mean velocity \bar{v} of the beam of atoms. Following the analysis given in [2], one obtains

$$\frac{\gamma\ell}{\bar{v}} \gtrsim 500. \quad (1)$$

Physically, (1) means that each atom has to undergo at least 500 elastic collisions during its propagation through the magnetic guide.

Our experiment aims at implementing this scheme for a beam of ^{87}Rb atoms. Its success relies therefore upon two preliminary and separate accomplishments. First, one has to build a source of cold atoms as intense as possible, with the lowest possible mean velocity. Second, one has to inject the atomic beam produced by this source into a long magnetic guide with minimal transverse and longitudinal heating. In the first section of this paper, we describe briefly the way we generate a high flux of atoms by means of a moving molasses [11] combined with transverse confinement. This configuration will be called the

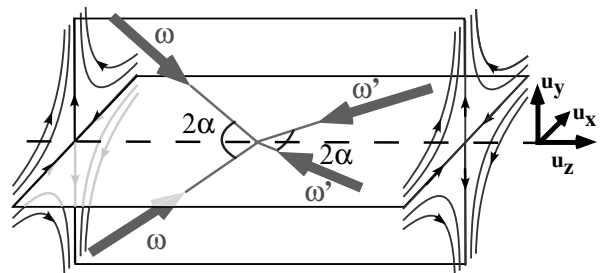


FIG. 1: Laser and magnetic configurations of the injecting MOT.

injecting MOT in the following. In the second section of the paper, we present the main features of our magnetic guide. In the third section, we focus on how to efficiently transfer atoms from the injector to the guide, and we report on the performances of our current experimental setup.

I. THE INJECTING MOT

The injecting MOT has been described in detail elsewhere [12] and we only recall its main features. It is based upon a four-beam laser configuration similar to the one used for the study of optical lattices described in [13], superimposed with a magnetic two-dimensional quadrupole field (see fig. 1).

The field vanishes along the z axis and the transverse gradient is typically $b' = 0.1$ T/m. The optical arrangement consists of four laser beams in a tetrahedral configuration. Each beam has a power of 25 mW and a waist of 12 mm. Two laser beams with frequency ω propagate in the yz plane along the directions $(\cos \alpha \mathbf{u}_z \pm \sin \alpha \mathbf{u}_y)$ with a positive helicity. The two other beams with frequency ω' propagate in the xz plane along the directions $(-\cos \alpha \mathbf{u}_z \pm \sin \alpha \mathbf{u}_x)$ with a negative helicity. The four beams are red-detuned with respect to the atomic transition $|5S_{1/2}, F = 2\rangle \rightarrow |5P_{3/2}, F = 3\rangle$, whose frequency

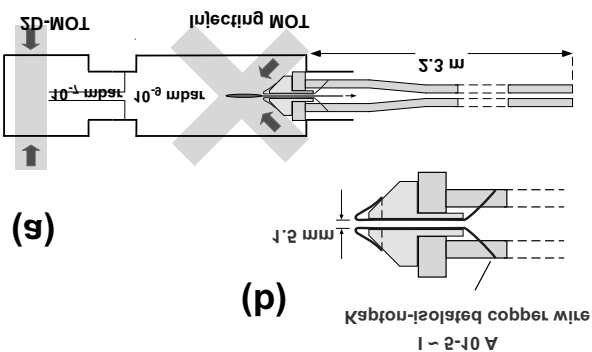


FIG. 2: (a) Schematic drawing of the experimental setup. (b) Miniature magnetic guide placed at the entrance of the magnetic guide.

is called ω_a . The average detuning $\delta = \bar{\omega} - \omega_a$, with $\bar{\omega} = (\omega + \omega')/2$, is typically -3Γ , where $\Gamma = 2\pi \times 5.9$ MHz denotes the natural width of the excited level of the transition. By properly choosing $(\omega - \omega')$, one can adjust the mean velocity \bar{v} from 0 to ~ 3 m/s.

The injecting MOT is set up in a rectangular glass cell ($130 \text{ mm} \times 50 \text{ mm} \times 50 \text{ mm}$). For most of the experimental results presented here, the atoms are captured from the low-pressure background gas (setup A). The partial pressure P_{87} for ^{87}Rb is measured by the absorption of a resonant beam. It can be varied from 10^{-9} mbar up to the saturated vapor pressure at room temperature (3×10^{-7} mbar) by controlling the temperature of the Rb-reservoir or the aperture of the intermediate valve. We find that the steady state flux Φ is independent of the average velocity of the beam. This flux is proportional to P_{87} in the range $10^{-9} \text{ mbar} < P_{87} < 10^{-8} \text{ mbar}$, and we obtain:

$$\Phi = 10^9 \text{ atoms/s for } P_{87} = 10^{-8} \text{ mbar.}$$

We have just completed the construction of a new apparatus (setup B, see fig. 2(a)) which has some advantages over this original system. This apparatus is based on the same principle as setup A, but it uses two separate magneto-optical traps. The first one is a two-dimensional magneto-optical trap (MOT) [14, 15] located in a chamber which has a relatively high pressure of rubidium vapor ($P \geq 10^{-7}$ mbar). The second MOT (the injecting one) is in a differentially pumped chamber where the pressure is very low ($P \leq 10^{-9}$ mbar). The first MOT generates a beam of cold atoms with an average velocity ~ 40 m/s; a significant fraction of this beam is captured by the injecting MOT and is subsequently slowed down and cooled. This allows us to limit the loss of atoms caused by collisions with background gas atoms while they propagate from the output of the injecting MOT to the entrance of the magnetic guide.

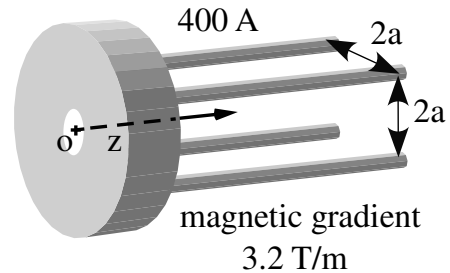


FIG. 3: Schematic drawing of the entrance of the magnetic guide. The hollow metal cylinder close to $z = 0$ allows for the connection of the electrical currents and the water cooling circuit circulating into the four copper tubes.

II. THE MAGNETIC GUIDE

The magnetic guide has a total length of 230 cm. It is made out of four copper tubes ($\mathcal{O}_{\text{ext}} = 6$ mm and $\mathcal{O}_{\text{int}} = 4$ mm) placed in a quadrupole configuration (see fig. 3). The tubes are located in the domain $z > 0$ and they are joined in $z = 0$ by a hollow metal cylinder, which allows for the circulation of current and cooling water from tube to tube. The axes of the copper tubes are placed at coordinates $x = \pm a$; $y = \pm a$, with $a = 7$ mm. A current $I = 400$ A is sent through the tubes, which provides, far from the entrance of the guide (*i.e.* $z \gg a$), a magnetic gradient $b' = 3.2$ T/m in the xy plane. The transverse magnetic gradient at the edge of the magnetic guide decreases quite fast (typical length scale $\sim a$), so it does not affect the operation of the injecting MOT.

A narrow glass tube ensures differential pumping between the cell of the injecting MOT and the chamber of the magnetic guide, where the residual pressure has to be minimized to avoid losses due to collisions with the background gas. We estimate that the pressure in this chamber is $\sim 4 \times 10^{-10}$ mbar, which corresponds to a lifetime ~ 20 s for the magnetically guided atoms.

III. TRANSFER FROM THE INJECTING MOT TO THE MAGNETIC GUIDE

We now present the various schemes that we have investigated to transfer the cold atomic beam generated by the injecting MOT into the magnetic guide. Eq. (1) shows that we need a guided beam as intense and cold as possible (a large collision rate γ) and at the same time a very low mean velocity \bar{v} . We note that, due to the presence of the metal cylinder located at the entrance of the magnetic guide (see fig. 3), the shortest distance between the output of the injecting MOT and the entrance of the magnetic guide is $D \sim 25$ mm. In other words, the injecting MOT is located in the region $-45 \text{ mm} < z < -25 \text{ mm}$ and the atoms have to travel over a distance of 25 mm before being captured by the magnetic guide provided

that they are in a magnetic sublevel corresponding to a low-field seeking state.

A. Free-flight transfer

The simplest way to load atoms from the injecting MOT into the guide consists in letting the atoms propagate freely between the two. In this purpose, we place a laser tuned to the $|5S_{1/2}, F=2\rangle \rightarrow |5P_{3/2}, F=2\rangle$ transition in the region $-25 \text{ mm} < z < 0$. The repumping laser is blocked in this transfer region, so that the extra “depumping” laser beam optically pumps the atoms in the $F=1$ ground state. Therefore, provided that the three magnetic levels $m=0, \pm 1$ of the $|5S_{1/2}, F=1\rangle$ are equally populated, we expect that one third of the atoms (state $m=-1$) emerging from the injecting MOT can be captured by the magnetic guide.

1. Constraints for free-flight transfer

Due to our experimental geometry, there are two issues that limit the use of a free flight transfer:

- It is restricted to relatively large velocities $\bar{v} > 1.5 \text{ m/s}$. Otherwise the free-fall due to gravity, $gD^2/(2\bar{v}^2)$, is so large that the coupling to the guide becomes velocity-dependent.
- During the free flight, the atom jet spreads transversally, which leads to a strong increase of the transverse temperature T_{\perp} in the guide, as compared with the temperature in the injecting MOT. Consider for instance a beam emerging from the injecting MOT with $\bar{v} = 2 \text{ m/s}$ and $T_{\perp} = 100 \mu\text{K}$. At the entrance of the magnetic guide, the radius of the beam is $R \sim (D/\bar{v}) \sqrt{k_B T_{\perp}/M} \sim 1.2 \text{ mm}$ (M is the atomic mass). The corresponding magnetic energy is

$$E_{\text{mag}} \sim \mu b' R \sim (D\mu b'/\bar{v}) \sqrt{k_B T_{\perp}/M}. \quad (2)$$

This gives $E_{\text{mag}}/k_B \sim 1 \text{ mK}$ in the present case.

2. Pulsed versus continuous mode

The operation of the injecting MOT in a continuous mode imposes to search for a compromise between two different requirements. For an efficient loading one has to take a relatively small detuning ($\delta \sim -3\Gamma$), so that the trapping force is large. On the contrary, in order to minimize the temperature of the outgoing atomic beam, a much larger detuning ($\delta \sim -7\Gamma$ for our laser intensity) is preferable.

A pulsed operation of the injecting MOT may provide, for a given application, an output beam with better characteristics than this compromise. First, one loads the

injecting MOT with the detuning which maximizes the capture rate R and with a zero launch velocity ($\omega = \omega'$). During this phase of duration t_1 , the number of trapped atoms varies according to $N(t) = (R/\gamma)(1 - e^{-\gamma t})$, where γ^{-1} is the mean escape time. One then switches the detuning of the trapping lasers to a much larger value, with $\omega \neq \omega'$ set to provide the required velocity \bar{v} . This launching phase must last a time t_2 so that all trapped atoms can leave the injecting MOT and reach the magnetic guide. For a trap of length L and a distance D between the trap exit and the guide, one has $t_2 = (L+D)/\bar{v}$. The optimization of t_1 depends on the values of γ and the launching time t_2 . For a low Rb vapor pressure (small R and small γ), the largest flux corresponds to

$$\gamma t_2 \ll 1 \quad : \quad \Phi \simeq R \quad \text{for} \quad t_1 = \sqrt{2t_2/\gamma}. \quad (3)$$

In this case, the flux Φ in the guide is equal to the capture rate of the injecting MOT and the operation in pulsed mode does not lead to a loss in efficiency. If we increase the Rb vapor pressure in the cell and thus the rate R so that $\gamma \sim t_2^{-1}$, the optimum operation of the pulsed mode corresponds to

$$\gamma t_2 \sim 1 \quad : \quad \Phi \sim 0.3 R \quad \text{for} \quad t_1 \sim t_2 \sim \gamma^{-1}. \quad (4)$$

This pulsed mode also makes the extraction of atoms from the injecting MOT much easier. Indeed, the optical pumping of the atoms to the hyperfine level $F=1$ is not total, because of the stray light present at the repumping frequency $|5S_{1/2}, F=1\rangle \rightarrow |5P_{3/2}, F=2\rangle$. Therefore, after leaving the injecting MOT, the atoms may still be deflected by the residual radiation pressure force resulting from an imbalance between the intensities of the various laser beams. This spurious effect is strongly decreased if the detuning of these lasers is increased to a value $\delta \sim -7\Gamma$ while the atoms travel in the “dangerous” region.

Finally, we note that, although the atomic beam is pulsed at the entrance of the guide, the pulses broaden as they propagate because of the longitudinal velocity dispersion Δv . This entails that a quasi-continuous beam is obtained after a distance $\sim L\bar{v}/\Delta v$ if one chooses $t_1 \sim t_2$.

B. Use of an auxiliary MOT

Some of the difficulties associated with the free-flight transfer can also be circumvented if we place an auxiliary guiding trap in the region $-25 \text{ mm} < z < 0$. This trap is a pure 2D MOT, whose beams are orthogonal to the z axis and illuminate points up to 4 mm from the entrance of the magnetic guide (see fig. 4). The transverse extension of the atomic beam at the entrance of the magnetic guide is then drastically reduced. As for the free flight transfer, we place a depumping laser at the entrance of the guide. The atoms are then trapped in the magnetic sublevel $F=1, m=-1$.

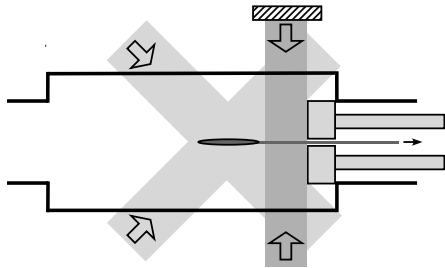


FIG. 4: Use of an auxiliary 2D MOT to transfer the atoms from the injecting MOT to the magnetic guide.

The disadvantage of this auxiliary trap concerns the broadening of the longitudinal velocity distribution, due to the random recoils associated with the spontaneous emission of photons as the atoms cross the auxiliary trap. The longitudinal heating remains relatively weak for high atomic velocities and large detunings δ_2 of the auxiliary MOT. An upper limit for $|\delta_2|$ is given only by the condition that the radiative force of the auxiliary MOT has to overcome the spurious radiation pressure imbalance which exists in the wings of the injecting MOT's laser beams, as discussed above.

C. Experimental results

We now present the experimental results that we have obtained concerning the characteristics of the guided atomic beam, in terms of temperature and flux. All these measurements have been performed using the setup A, *i.e.* with a vapor-loaded injecting MOT.

1. Longitudinal velocity distribution

The measurement of the longitudinal velocity distribution is quite straightforward if we operate the injecting MOT in pulsed mode, since we can derive the longitudinal temperature directly from the temporal width of the absorption signal when a given atom pulse passes through the probe beam. This beam is located downstream, at a distance of either 40 cm or 200 cm from the entrance of the magnetic guide.

When operating in pulsed mode, we measure a longitudinal temperature in the range 50-100 μK . The lowest temperatures are obtained for large velocities ($\bar{v} = 2.6$ m/s). This effect is probably due to the heating of the atoms by the stray light of the various trapping beams, when they travel over the distance D between the injecting MOT and the guide. This heating is larger if the atoms spend more time in this region, *i.e.* if they are slow. The presence of the auxiliary MOT causes some additional heating of the atomic beam, proportional to the time spent by the atoms in the laser beams. For

$\delta_2 = -6.5 \Gamma$, the increase of the longitudinal temperature of the beam is at most 30%, while, as we shall see, the transverse temperature decreases by an order of magnitude, thanks to the auxiliary MOT.

When the injecting MOT is operated in continuous mode, we found much larger longitudinal temperatures, in the range of 0.5–1 mK. We think that this is due to the acceleration and heating of the atoms when they travel between the injecting MOT and the guide, the heating being much more dramatic than in the pulsed mode, since the frequencies of the trapping beams are closer to resonance.

2. Transverse temperature

We have measured the transverse temperature in the guide in two ways, which give consistent results. First, we have scanned transversally the position of the probe laser beam and reconstructed the transverse profile of the atomic beam. Alternatively, we have used radio-frequency evaporation to selectively remove a fraction of the atomic distribution. From the variation of the fraction of remaining atoms as a function of the radio-frequency, we infer the transverse temperature of the atomic beam (see Appendix).

Using the auxiliary MOT, we find a temperature ranging from 100 μK to 200 μK . We have obtained similar results for the continuous and pulsed regimes. The variation of the transverse temperature with the magnetic gradient b' and the longitudinal velocity is in good agreement with the estimate (2), where D should be replaced by the distance $D' \sim 4$ mm between the exit of the auxiliary MOT and the entrance of the magnetic guide.

In absence of the auxiliary MOT, we have measured much larger transverse temperatures inside the guide, in the range of 1-2 mK. This is a consequence of the increase of the beam's transverse size at the magnetic guide entrance, after free propagation over the distance D . The variation of the transverse temperature with b' and \bar{v} is also in good agreement with the prediction (2).

3. Flux

The flux of atoms in the magnetic guide is not significantly modified by the presence of the auxiliary MOT. Operating in continuous mode at a pressure $P_{87} = 10^{-8}$ mbar, we find that this flux varies between 1.5×10^8 and 3×10^8 atoms/s, when \bar{v} varies between 1.5 m/s and 3 m/s. This corresponds to a transfer efficiency between 15% and 30%. Similar values are achieved in pulsed mode if we optimize the loading time t_1 according to (3).

For velocities smaller than 1.5 m/s, we did not find that a significant fraction of the atoms emitted by the injecting MOT could be transferred to the magnetic guide. We attribute this fact to the depletion of the slow atomic beam by collisions with atoms from the rubidium vapor

in the cell. The slow atoms have to travel over a distance ~ 10 cm through the cell and the tube ensuring the differential pumping, before they arrive in the ultra-high vacuum region of the magnetic guide. For $P_{87} = 10^{-8}$ mbar (i.e. a total rubidium pressure 4×10^{-8} mbar) and $\bar{v} = 1.5$ m/s, we estimate the atomic flux to be reduced by 40 % over this distance. This limitation should be overcome with our new apparatus (setup B) as discussed at the end of § I.

D. Miniature guide

At low atomic velocities, the auxiliary MOT does not provide efficient coupling of atoms into the guide due to strong recoil heating in the longitudinal direction. For this reason, we have developed a miniature magnetic guide (MMG) on a conical supporting structure. The shape has been chosen in order to keep a good optical access for the injecting MOT's beams. The MMG is added at the entrance of the magnetic guide as depicted in fig. 2(b).

The MMG generates a two-dimensional magnetic quadrupole field by means of four elliptical Kapton-coated copper wires with a 1 mm^2 cross section. The wires are placed at coordinates $x = \pm b, y = \pm b$, with $b = 1.3$ mm. They provide a transverse confinement over a distance of 40 mm up to a point at which the confining force of the long magnetic guide has risen to its asymptotic value. The inner supporting structure of the wires is a tube with a diameter $d = 3$ mm, which also ensures differential pumping between the injecting MOT's chamber and the section of magnetic guide.

The recombination of the current between the wires of the MMG is done in a way as to minimize the free flight distance. Consequently, the transverse free expansion remains small. The longitudinal temperature is not affected in this case since no spontaneous emission processes occur. The wires emerge from the supporting structure before being folded back outwards and attached to the conical structure. The currents recombine in the metallic supporting structure to which the non-isolated wire ends are screwed (see fig. 2(b)). In this way the laser beams of the injecting MOT are not interrupted by the MMG's wires. The MMG allows to reduce the distance over which the atoms expand freely to less than 3 mm. The magnetic gradient is typically 1 T/m ($0.22 \text{ T m}^{-1} \text{ A}^{-1}$). The current running in the MMG has to be chosen in the same sense as the one in the guide. The wires of the MMG are kept cooled by thermal contact with the water-cooled magnetic guide. With a current of 5 A running through the wires of the MMG, we find an increase of resistivity that corresponds to a temperature rise of 5 K assuming an homogeneous temperature change of the wires.

In order to measure the mean velocity of the atoms along the longitudinal axis, we use as before a time-of-flight technique. We operate the injecting MOT in a

pulsed mode. At time $t = 0$, we launch a bunch of atoms which propagates in the magnetic guide, and we monitor the time-dependent absorption signal of a probe beam located further downstream. The MMG allows for the production of a very low velocity beam in the magnetic guide. We have recently observed atoms in the magnetic guide with a mean velocity of the order of 70 cm/s. For the production of such a low-velocity atomic beam, two requirements have to be met. The injecting MOT's beam profiles have to be balanced over the whole free-flight distance (otherwise the atoms are accelerated while passing through the wings of the laser beams). Furthermore, care has to be taken that the atoms are not pumped out of the $|F = 1, m_f = -1\rangle$ level by stray light while propagating in the magnetic guide. For that purpose, we detune the frequency of the repumping light by several line widths. Actually, we do not detect any atoms in the guide when the repumping laser is on resonance.

In conclusion, we have reported the continuous and pulsed loading of a slow and cold atomic beam into a magnetic guide. In order to optimize the transfer into the guide, we have investigated various coupling schemes. The first one is based on an auxiliary two-dimensional MOT that confines the atoms transversally before they enter the guide. However, for low atomic velocities, the atoms are strongly heated in the longitudinal direction. This limitation does not occur in another coupling method which relies on magnetic confinement in the transfer zone. For this purpose, we have constructed a miniature magnetic guide located between the injecting MOT and the long magnetic guide. The latter scheme allows to inject atoms with velocities down to 70 cm/s into the guide, a result which we hope to further improve in future experiments.

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APPENDIX A: TEMPERATURE MEASUREMENTS BY EVAPORATION IN THE COLLISIONLESS REGIME

The appendix is devoted to the determination of the transverse temperature from the fraction of remaining atoms when a radio frequency wave is applied. We restrict the analysis to the case of a collisionless gas. The atoms propagate freely along the guide axis (z) and they are confined in the transverse xy plane by an isotropic harmonic potential with frequency ω . The transverse and longitudinal motions are decoupled from each other and

the total Hamiltonian then reads:

$$H(\mathbf{r}, \mathbf{p}) = H_{\perp}(\mathbf{r}_{\perp}, \mathbf{p}_{\perp}) + \frac{p_z^2}{2m},$$

where the Hamiltonian for the transverse motion is:

$$H_{\perp}(\mathbf{r}_{\perp}, \mathbf{p}_{\perp}) = \frac{p_{\perp}^2}{2m} + \frac{1}{2}m\omega^2 r^2$$

with $p^2 = p_x^2 + p_y^2$, $r^2 = x^2 + y^2$. Another dynamical quantity of interest for the study of the transverse motion is the z -component of the angular momentum

$$\mathcal{L}(\mathbf{r}_{\perp}, \mathbf{p}_{\perp}) = xp_y - yp_x.$$

The trajectory of an atom is characterized by three constants of motion: the velocity v along the guide axis, the total (kinetic+potential) transverse energy $E = H_{\perp}(\mathbf{r}_{\perp}, \mathbf{p}_{\perp})$, and the z -component of the angular momentum $L = \mathcal{L}(\mathbf{r}_{\perp}, \mathbf{p}_{\perp})$. One readily establishes a relation between the two quantities E and L characterizing the transverse motion: $E \geq |L|\omega$. For a given (E, L) , the trajectory is confined in the region of space $r_{\min} \leq r \leq r_{\max}$ with:

$$r_{\min}^2 = \frac{E - \sqrt{E^2 - L^2\omega^2}}{m\omega^2} \quad r_{\max}^2 = \frac{E + \sqrt{E^2 - L^2\omega^2}}{m\omega^2}.$$

The evaporation is performed by inducing spin flips with a radiofrequency field of frequency ν on a surface defined by: $\mu|B(\mathbf{r}_{\text{evap}})| = h\nu$. Note that it does not mean *a priori* that atoms with an energy higher than $h\nu$ are evaporated. It depends actually on the total energy of the particle and on its angular momentum. Evaporation occurs only if $r_{\min} \leq r_{\text{evap}} \leq r_{\max}$, which means that the trajectory goes through the surface of evaporation. In the following, we note $E_0 = m\omega^2 r_{\text{evap}}^2$.

In order to determine the fraction f of atoms which is not affected by the evaporation, one needs to derive the density probability $P(E, L)$ for a given atom to have an energy E and an angular momentum L . By definition,

$$P(E, L) \propto \int d^2r d^2p e^{-\beta H_{\perp}} \delta(L - \mathcal{L}) \delta(E - H_{\perp}), \quad (\text{A1})$$

where $\beta = 1/(k_B T)$. One readily obtains [16]:

$$P(E, L) \propto e^{-\beta E} \Theta(E - |L|\omega),$$

where Θ is the Heaviside step function. We distinguish two categories of atoms that are not affected by the radio-frequency wave:

- atoms such that $r_{\min} > r_{\text{evap}}$, the corresponding range of values for E and L is denoted \mathcal{D}_1 ;
- atoms such that $r_{\max} < r_{\text{evap}}$, the corresponding range of values for E and L is denoted \mathcal{D}_2 .

The fraction f of non-evaporated atoms is obtained after a simple calculation and it reads:

$$f = \int_{\mathcal{D}_1 \cup \mathcal{D}_2} P(E, L) dE dL = 1 - \sqrt{\frac{\pi\beta E_0}{2}} e^{-\beta E_0/2}. \quad (\text{A2})$$

The temperature is obtained by fitting the experimental data to the function (A3). This fraction has a minimum for $r_{\text{evap}} = (\beta m\omega^2)^{-1/2}$ equal to $f_{\min} \simeq 0.2398\dots$ Without elastic collisions, it is impossible to evaporate all atoms. On the other hand, since collisions allow the redistribution of angular momentum and energy, the observation of a fraction of non-evaporated atoms lower than f_{\min} is a signature of the presence of elastic collisions in the sample when crossing the region where evaporation is applied. We emphasize that this treatment is valid only if the magnetic potential is close to a harmonic potential: $k_B T \ll \mu B_0$, where T is the temperature, μ the magnetic moment and B_0 the longitudinal bias field applied in the evaporation region. When this criterium is not fulfilled, we have to use a numerical model based on a Monte-Carlo sampling of the atomic distribution rather than the analytical expression (A2).

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